Synchronization

Mutual Exclusion

- Mutex = mutual exclusion
- “ensure that multiple process that share resources do not attempt to share the same resource at the same time”
- “The concurrent access to a shared resource by several uncoordinated user-requests is serialized to secure the integrity of the shared resource”
- How can this be accomplished for distributed system?

Critical Section

- A critical section (CS) is “a code segment in which a shared resource is referenced” and “the portion of code or program accessing a shared resource”
- We must prevent concurrent execution by more than one process at a time
  - **Mutual exclusion** is one part of the solution to this problem
- Requirements:
  - If no process is in the critical section, any requesting process may access it without delay
  - When two or more process want the critical section, a section of which process to enter the critical section **cannot be delayed indefinitely**
  - No process can prevent another process from entering the critical section **indefinitely**

Critical Section Problem

- Consider a system consisting of n processes \( \{P_0, P_1, P_2, \ldots, P_n\} \)
  - Each process has a segment of code, called a critical section
  - The important feature of the system is that, when one process is executing in its critical section, no other process is to be allowed to execute in its critical section
  - The execution of critical sections is mutually exclusive in time
- Assume we have several sequential processors
  - Let these processors share a common data area (i.e., data within a shared memory)
  - This is the same as multi-programmed processes or cooperating sequential processes
Critical Section Problem

- Assume that each process has the following code:
  
  ```
  P_i() {
    while (true) {
      criticalSection_i;
      program_i;
    }
  }
  ```

  - Within `criticalSection_i`, the common data area is referenced (i.e., data within the shared memory)
  - Only one process can be in its critical section at any given time
  - Such processes may be called **loosely connected processes**. They are almost independent.

Critical Section Solutions

- Critical Section Solutions (Galli00)
  - The solution must ensure the two processes do not enter critical regions at the same time
  - The solution must prevent interference from processes not attempting to enter their critical regions
  - The solution must prevent starvation

- Critical Section Solutions, alternate statement (SilGal98)
  - A solution to the critical section problem must show that
    - Mutual exclusion is preserved
    - Progress requirement is satisfied
    - Bounded-waiting requirement is met

Critical Section Problem

- Assumptions:
  1. Only one process can access the shared memory at a time, simultaneous references would result in sequential accesses in an unknown order
  2. There is no priority among the critical sections
  3. Processors can be of different speeds (We don’t want to depend on timing tricks)
  4. A process can halt, only if it is not in its critical section

- Now assume that the process all begin at the same time
  
  ```
  begin
    P_1 and P_2 and P_3 and ... and P_n
  end
  ```
Critical Section Solutions

- How is mutual exclusion preserved?
  - If process \( P_1 \) is executing in its critical section, then no other processes can be executing in their critical sections.

- How is the progress requirement satisfied?
  - If no process is executing in its critical section and there exist some processes that wish to enter their critical sections,
  - Then only those processes that are not executing in their remainder section can participate in the decision of which will enter its critical section next,
  - And this section cannot be postponed indefinitely.

- How is bounded waiting met?
  - There exists a bound on the number of times that other processes are allowed to enter their critical sections.
  - After a process has made a request to enter its critical section
  - And before that request is granted.

Critical Section Hardware Solutions

- Hardware mechanism:
  - Needed are some atomic hardware operations
    - that atomically test if a critical section is currently occupied
    - That can grab it if it not busy
    - And otherwise will wait, while continuing to test it until it is not busy
  - Possible solutions include
    - Atomic hardware operations
    - Hardware locks
    - Spin locks
    - Mutex hardware operations
    - Cache concurrency control

- In a uniprocessor,
  - The CS can disable/enable interrupts whenever a process enters/exits the CS

- In a multiprocessor or a distributed system
  - The uniprocessor solution won’t work since it can only affect the machine on which the CS lives
  - We need to use test-and-set mechanisms, busy-waiting, atomic swaps or some software solutions

- While atomic operations are difficult to implement in parallel computers (multiprocessors),
  - They are possible (e.g. spinlocks in the Encore Multimas)

- However, for distributed systems
  - The solutions need to be done in software

Critical Section Hardware Solutions

- Lock mechanisms:
  - A lock is one form of hardware support for mutual exclusion
  - If a shared resource has a locked hardware lock, it is already in use by another process
  - If it is not locked, a process may freely
    - Lock it for itself
    - Use it
    - Unlock it when it finishes
  - Problem: Race conditions
Critical Section Hardware Solutions

- Test-and-Set:
  - Is a hardware implementation for testing for the lock and resetting it to locked
  - If test shows unlocked, the process may proceed
  - Acts as an atomic operation
  - Permits
    - Busy waits
    - Spinning
    - Spinlocks

- Atomic Swap:
  - Performs three operations atomically
    1. Swap current lock value with temp locked lock
    2. Examine new value of temp lock
    3. If locked, repeat
    4. If unlocked, proceed into critical section/region
  - Utilizes a temporary variable

Critical Section Software Solutions

- Software mechanisms:
  - Possible software solutions include
    - Software locks
    - Programming language constructs
      - Semaphores
      - Critical regions
      - Monitors
    - System library support
  - In distributed systems mechanisms for critical section software solutions also include
    - Centralized lock manager algorithms
    - Distributed lock manager algorithms
    - Token-passing algorithms
    - Election algorithms

- Every algorithm used for software mutual exclusion solutions must meet the following criteria
  - Does mutual exclusion hold?
  - Is interference from other procedures or processes not currently trying to get into the critical section prevented?
  - Are all processes waiting for the shared resource (or critical section) protected against starvation? That is, will each process eventually be scheduled?
Centralized Lock Manager
- A centralized lock manager maintains information on:
  - Which processes have requested access to critical section
  - Which processes have been granted request
- A centralized lock manager algorithm:
  - Request message (required)
    - When a process needs to access CS, it sends a request message to the centralized lock manager, requesting entry to CS
  - Granted message (required)
    - If CS is available, the lock manager returns a granted message to the requesting process
  - Queued message (optional)
    - If CS is not available, the lock manager may return a queued message, in some versions of this type of algorithm
  - Release message (required)
    - When a process that has been granted access to a CS finishes CS, it sends a release message back to the lock manager so that another process can be granted access

Correctness of the algorithm
- Does the algorithm assure mutual exclusion?
  - Yes, as only one process is granted access at a time, and no other process can enter its critical section until the first process finishes and sends a release message
- Can other processes not in competition for the critical section interfere with access to the critical section?
  - No, as only processes requesting or using the critical section communicate with the lock manager
- Is starvation possible?
  - No, as unfulfilled requests are queued until granted access

Problems/Disadvantages
- The lock manager is a single critical component
  - There is no redundancy. The single lock manager may crash and bring down entire system.
  - If it goes down, all processes dependent on it may go down as well
- This means there is a single point of failure
  - This would be unusable for real-time systems
- Since all messages are sent to the lock manager or received from the manager
  - There is increased traffic to/from that node
  - This creates a possible bottleneck in the network

Example
- Now consider a distributed system with three running processes, Process1, Process2, Process3
- Each of the processes has access to a shared data
- Each process has a critical section
- Assume the mutual exclusion is controlled by a centralized lock manager
Centralized Lock Manager

- Initially no processes are in their critical section
  a. Process 3 requests its CS and
  b. Process 3 granted access to its CS
  c. Process 1 requests its CS but the CS is locked, so
  d. Process 1 is placed on a queue waiting for the lock
  e. Process 2 requests its CS but the CS is locked, so
  f. Process 2 is queued
  g. Process 3 finishes its CS, releasing access to the CS and opening the lock
  h. The central manager checks the lock, finding it unlocked and Process 1
     is granted access to its CS by the central manager
  i. Process 1 finishes its CS releasing access to the CS and opening the lock
  j. The central manager checks the lock, finding it unlocked and Process 2
     is granted access to its critical section by the central manager
  k. Process 2 finishes its CS releasing access to the CS and opening the lock

Distributed Lock Manager

- A distributed lock manager avoids both the central point of failure and the network traffic hotspot problems
- A distributed lock manager algorithm:
  - Request message (required)
    a. When a process needs to access its critical section, it sends a request message with its current timestamp to all the other processes, requesting entry to the critical section. This may be done as a broadcast message or as a set of individual messages.
  - Queued message (optional)
    a. If another process is in the critical section, that process queues the request and may return a queued message, in some versions of this type of algorithm. This optional message helps distinguish between those processes that are very busy with other requests and those that have died.
  - Granted message (required)
    a. If any of the other processes are not in the critical section and have no other request with an earlier timestamp waiting in their queue, they return a granted message to the requesting process
    b. If another process is in its critical section, it queues the requests of all other processes until it is done. Then it sends out a granted message to every process in its queue, much like a release message.
    c. This means that a process may enter its critical section only if it has received granted messages (or votes) from the majority of the other processes. (Note that it is not necessary to receive an unanimous vote. Why?)
- Correctness of the algorithm
  - Does the algorithm assure mutual exclusion?
    a. Yes, as only one process is granted access at a time by the majority of all other processes.
    b. Two or more processes cannot receive a majority of the votes at the same time
  - Can other processes not in competition for the critical section interfere with access to the critical section?
    a. No, as it only requests a vote from a majority of the other processes.
    b. However, without the queued message, it is possible that a large number of failed processes could prevent a process from proceeding into its critical section.
  - Is starvation possible?
    a. No, as unfulfilled requests are queued in order of timestamp until granted access.
Distributed Lock Manager

Problems/Disadvantages

- While the lock manager is no longer a single critical component, all processes now take part in granting a critical section request. If a majority of the processes fail, the other processes could deadlock waiting for a decision.
- This is one reason the queued messages are used. If a process never receives a queued message from another given process (perhaps after several request), it knows that process must be dead. Thus the number of processes needed for a majority vote may be reduced.
- Furthermore, far more messages are generated by this algorithm. As a process leaves its critical section, it sends out granted messages to all process quests in its queue. These same processes may send out queued messages as responses to all request messages as well.
- This means we have far more traffic on the network as a whole, instead of just one network hotspot.

Token-Passing Mutual Exclusion

- There are many token-passing algorithms that may be used on parallel or distributed systems
- The network of processors must be logically arranged as a ring of processors.
- There is only one unidirectional path through the ring.
- Only one token is active in a logical ring of processes.
- When a process holds the token, it may enter its critical section. Otherwise, it passes the token onto the next logical process in the ring.
- When the process is done with its critical section, it passes the token onto the next process.

Token-Passing Mutual Exclusion

Correctness of the algorithm

- Assure mutual exclusion?
  - Yes, there is only one token.
  - Only one process can hold the token at a time.
- No interference from processes not needing mutex?
  - Yes, if a process does not need mutual exclusion, it simply passes the token on.
- Possible starvation?
  - No, a process holding the token may enter mutual exclusion only once.
  - Then, it must pass the token on to the next process.

Complications

- What is the token gets lost?
  - How might that happen?
  - How can you tell if that happens?
  - How do you know that the token is not just being used for a long time?
- What is the process holding the token crashes?
- What is some other process crashes?
  - Is the ring destroyed?
- How can we add (and identify) other processes to the ring?
- How can we remove some processes from the ring?
Token-Passing Mutual Exclusion

Possible Solutions
- Make one centralized node be a monitor (synchronized object) and/or make the token a monitor
  - Send messages to request the current location of the token
  - If the token is missing, start a new token
  - All new nodes (and recovered nodes) should check in with the monitor
  - Lost nodes can be recorded in the monitor via the neighbors of the lost nodes
- Make all nodes be monitors

Tree-Based Token Algorithm for Mutual Exclusion

This algorithm is a distributed algorithm, implemented with a global FIFO queue.
- Local FIFO queues are linked to form a global queue using a tree topology.
- Recall in the Token-Ring algorithm that the token was passing around the ring even when no node wanted or needed it.

An alternate approach would be as follows:
- A process requests the token whenever it needs it
- The token only moves to another node when it is requested.
- The process's request message must find the node on which the token is located.
- In the topology of a tree, other nodes can always find the root by traveling back up through their ancestors.

Tree-Based Token Algorithm for Mutual Exclusion

The rules are quite simple.
- The token is always located at the root of the tree.
- The tree is considered a directed graph with the arcs all pointing toward the root.
- Each node of the tree represents the current logical location of a process.

The algorithm works as follows
1. Whenever a node's process wants mutual exclusion (the token) it sends the request to the root of the tree.
2. When the token is acquired, it must first move to the requesting node. In doing so, it reshapes the tree so that the requesting node becomes the root of the tree.
3. Each process maintains a FIFO queue of requests and a pointer to its parent in the tree.
4. Whenever a request is made, it is appended to the FIFO queue at that node.
5. If the node does not currently have the token and the queue is empty, then node (process) must send the request to its parent node.
6. If the node does have the token and the FIFO queue is not empty, the process removes the top entry in the queue and sends the token to that node (process), while changing the direction of its own pointer to point toward the process when the token is sent.
Tree-Based Token Algorithm for Mutual Exclusion

- Correctness of the algorithm
  - Assure mutual exclusion?
    - Yes, there is only one token.
  - Only one process can hold the token at a time.
  - No interference from processes not needing mutex?
    - Yes, a token only moves to those nodes that request it (mutual exclusion).
  - Possible starvation?
    - No, a process wanting the token will be placed in a FIFO queue, and it will eventually be granted the token.

Recall that a tree is just an acyclic graph, meaning it is not possible to form a cyclic wait. This prohibits deadlock.

Example

1. Initially, P0 holds the token. Also, P0 is the current root.

2. P3 wants the token to get into its critical section. So, P3 adds itself to its own FIFO queue and sends a request message to its parent P2.

3. P2 receives the request from P3. It adds P3 to its FIFO queue and passes the request message to its parent P1.

4. P1 receives the request from P2. It adds P3 into its FIFO queue and passes the request message to its parent P0.

5. At this point, P2 also wants the token. Since its FIFO queue is not empty, it adds itself to its own FIFO queue.

6. P0 receives the request from P3 through P1. It surrenders the token and passes it on to P1. It also changes the direction of the arrow between them, making P1 the root, temporarily.

7. P1 removes the top element of its FIFO queue to see which node requested the token. Since the token needs to go to P3, P1 surrenders the token and passes it onto P3. It also changes the direction of the arrow between them, making P3 the root.

8. P2 removes the top element of its FIFO queue to see which node requested the token. Since the token needs to go to P3, P2 surrenders the token and passes it onto P3. It also changes the direction of the arrow between them, making P3 the root.

9. Now, P3 holds the token and can execute its critical section. It is able to clear the top (and only) elements of its FIFO queue. Note that P3 is the current root.

10. In the meantime, P2 checks the top element of its FIFO queue and realizes that it also needs to request the token. So, P2 sends a request message to its current parent, P3, who appends the request to its FIFO queue.
Tree-Based Token Algorithm for Mutual Exclusion

11. As soon as P3 completes its critical section, it checks the top element of its FIFO queue to see if it is needed elsewhere. In this case, P2 has requested it, so P3 sends it back to P2. It also changes the direction of the arrow between them, making P2 the new root.

12. P2 holds the token and is able to complete its critical section. Then it checks its FIFO queue, which is empty. So it waits until some other node requests the token.

Election Algorithms

- Many of the algorithms for distributed systems require some centralization, some site with leader/coordinator activities.
- All other sites need to recognize this leader; often this is accomplished by an initial agreement/election.
- When the site of the leader fails or goes down for some reason, it is necessary to elect a new leader.
- This is the purpose of election or agreement algorithms.

- Assumptions for most election algorithms
  - A complete topology, i.e., one message hop between any two processes
  - All process IDs are unique and known to all other processes.
  - All communication networks are reliable, i.e., only communicating processes may fail.
  - This assures that no messages are
    - Lost
    - Duplicated
    - Corrupted
  - A recovering process is aware that it failed
    - Failure is reliably detected by setting the time-out interval to be a little larger than the sum of the round-trip message delay and the message processing time.
    - A failed process can rely on the coordinator to poll periodically for recovered process so that they may rejoin the pool of processes.

- There are two basic criteria for an election algorithm.
  - One way to decide the leader is to use some global priority.
    - The Bully algorithm by Garcia-Molina (1982)
  - The second is a more general, preference-based algorithm, that permits some nodes to have heavier votes.
    - Token-Ring election algorithm by Chang & Robert
Bully Election Algorithm

- The Bully Election Algorithm (Garcia-Molina)
  - One process notices that the leader/server is missing and
    - Sends messages to all other processes
    - Requests to be appointed leader
    - Includes his processor number
  - Processes with higher (lower) process numbers can bully the first process.
  - The process with highest ID wins the election and sends out a message to that effect.
  - The process that initiates the election need only send messages about election to higher numbered processes.
  - Any processes that respond effectively tell the first process that they overrule him and that he is out of the running as they have higher IDs.
  - These processes then start sending election messages to the other high-number processes.

1. We start with 6 processes, all directly connected to each other. P6 is the leader, as it has the highest number.

2. P6 fails

3. P3 notices that P6 does not respond. So it starts an election, notifying those processes with IDs greater than 3.

4. Both P4 and P5 respond, telling P3 that they’ll take over from here.

5. P4 sends election messages to both P5 and P6.

6. Only P5 answers and takes over the election.

7. P5 sends out only one election message to P6.

8. When P6 does not respond, P5 declares itself the winner.
Token-Ring Election Algorithm

- Token-Ring Election Algorithm (Chang & Roberts)
  - Each process has a unique ID. Each process knows its successor in the ring.
  - When a process notices the leader is down, it sends an election message to its successor.
  - If the successor is down, the originating process sends the message to the next process in the logical ring.
  - Each process that receives an election message, passes it on to the next process in the ring. Each sender appends its own ID to the message.
  - The election message eventually returns to the originating process and contains its ID.
  - At this point, the election message is changed to a coordinator (new leader) message and sent around ring. The process with the highest ID in the circulated election message becomes the new leader.
  - When the coordinator message comes back to the originating process, it is deleted.

Token-Ring Election Algorithm

1. We start with 6 processes, connected in a logical ring. P6 is the leader, as it has the highest number.

2. P6 fails

3. P3 notices that P6 does not respond. So it starts an election, sending a message containing its ID to the next node in the ring.

4. P5 passes the message on, adding its own ID to the message.

5. P0 passes the message on, adding its own ID to the message.

6. P1 passes the message on, adding its own ID to the message.

7. P4 passes the message on, adding its own ID to the message.

8. When P3 receives the message back, it knows the message has done around the ring, as it own ID is in the list. Picking the highest ID in the list, it starts the coordinator message “5 is the leader” around the ring.

9. P5 passes on the coordinator message.
**Token-Ring Election Algorithm**

10. P0 passes on the coordinator message.

11. P1 passes on the coordinator message.

12. P4 passes on the coordinator message.

13. P3 receives the coordinator message, and stop it.

**Global Clocks**

- Distributed systems have no global clock
- Each processor in the system is autonomous
- Each processor has its own clock
- Impossible to have the processes across the system synchronized exactly
- Cannot know the true time order of any two events

**Ordering of Events**

- It is impossible to know which of two events happens first
- This has an impact on scheduling
- This makes the distributed system harder to debug

**Global Time via Shared Memory?**

- Distributed systems have no shared memory
- Thus it is hard (impossible) to get an up-to-date state of the entire system
- A global state would give us
  - A view of all local states
  - The contents of all messages currently in transit
Definitions

- **Drifting**: “the gradual misalignment of once synchronized clocks caused by the slight inaccuracies of the time-keeping mechanisms” *(Galli)*
- **Clock Skew**: “the difference in time between two clocks due to drifting” *(Galli)*

Global Time via Physical Clocks?

- **Universal Time Coordinator (UTC)**
  - A consensus
  - Accurate to +/- 1 second per 20,000,000 years
  - About 1 part in 10^12
  - Sources:
    - Geostationary Operational Environmental Satellites (GEOS)
    - GPS devices
    - WWV: a Fort Collins radio station

Global Time via WWV

- **A Fort Collins shortwave radio station**
  - Transmits UTC signal
  - Low-frequency => less atmospheric disturbance
  - 2000 mile radius
  - Sends signals once a day to clocks/watches
  - Transmission delay is 24000 microseconds at the extreme range
    - Less than 0.1 second
    - Can be corrected for

UTC Time Providers

- **Time Provider**: “a commercial device that is capable of directly receiving information from a UTC server and making appropriate adjustments due to communication delays” *(Galli)*
- Such devices are currently installed in watches, clocks, and computers
Network Delays when Communicating Time

Correcting for Transmitted Time

- A UTC signal is sent out
- Transmit time varies depending on
  - Atmospheric conditions
  - Humidity
- Receiving clock must make compensation for transmit time
- However, once reset, clock will start drifting again

Forward Adjustment of a Clock

Physical Time Services

- Centralized
  - Broadcast-based
    - UTC (previous slides)
    - Berkeley Unix algorithm
  - Request-driven
- Distributed

**Notice**: clocks cannot be moved backward
Berkeley Unix Algorithm

- Gusella & Zatti (1989)
- Synchronizes clocks for processors running Berkeley Unix 4.3
- Does not require UTC
- Centralized server broadcasts time periodically

The Berkeley Algorithm for Physical Clock Synchronization

1. Current time = 740
2. My current time is 720
3. My current time is 742
4. Adjust forward 7
5. Adjust slowdown to accommodate 5

Request-Driven Physical Clock Synchronization

Location A
- Current time = 737
- RCV = 740
- Adjusted time = 750
- New current time = 750

Time Server
- Request for current time
- Current time = 740

Distributed Physical Time Services

- Each processor broadcasts its current time at regular intervals
- Then starts a timer
- Timestamps each response
- Does so until timer runs out
- Then adjusts its own time accordingly
Fault-Tolerant Threshold Method

Discard $m$ Highest and Lowest Values

Network Time Protocol (NTP)
- Currently version 3
- RFC 1305 (request for comments)
- Design goals
  - Allow accurate UTC synchronization
  - Enable survival despite significant losses of connectivity
  - Allow frequent resynchronization
  - Protect against malicious or accidental interference

Request-Driven Time Service
- Cristian (1989)
- Uses a threshold to remove bad times caused by slow/faulty message transmission
- Threshold matched against difference of times in current processor and received from server
- Considers transmit time and interrupt time
Strata in the NTP Architecture

Simple Network Time Protocol (SNTP)
- An adaptation of NTP
- Simplifies access to an NTP server
- RFC 1769
- Clients located only at the highest strata
- SNTP servers do not implement fault tolerance

Logical Time
- Because of clock skew, physical clocks do not provide absolute time ordering of events
- Instead we use the concept of virtual time to order certain events
- There are a great number of algorithms that attempt to provide logical time and some event ordering
  - E.g. Lamport’s paper

Ordering Events
- What is an event?
  - Sending a message
  - Receiving a message
  - Execution within a process
- Most events happen asynchronously
  - Non-instantaneous communication
  - Interruptions
- There is no global state
Assumptions

- Assume all processes are sequential
- Assume that the sending of a message always precedes the receiving of said message
- Need to define a relationship that combine this information
  - Lamport’s \( \rightarrow \) “happens before” relation

Properties of \( \rightarrow \)

1. \( a \rightarrow b \) is defined as
   - If \( a \) and \( b \) are in the same process, then \( a \) happens before \( b \) happens
   - If \( a \) is sending a message, then \( b \) is receiving the same message
2. Transitive: If \( a \rightarrow b \) and \( b \rightarrow c \), then \( a \rightarrow c \)
3. If there is no ordering between \( a \) and \( b \), \( !(a \rightarrow b) \) and \( !(b \rightarrow a) \), then \( a \) and \( b \) are concurrent (disjoint)

Happen-Before Relationship Examples

Properties of a Logical Clock

- Let \( C_i \) be associated with the process \( P_i \), for all processes \( P_i \)
- Clock condition:
  - if \( a \rightarrow b \), then \( C(a) \rightarrow C(b) \)
- Subconditions:
  - If \( a \rightarrow b \) in process \( P_i \), then \( C_i(a) < C_i(b) \)
  - If \( a \) sends message \( m \) and \( b \) receives \( m \), then \( C_i(a) < C_j(b) \)
Logical Clock Conditions

- In order to achieve these conditions,
  - Process Pi increments Ci between any two events related to Pi
  - If a is sending message m from Pi, put a timestamp, $T_m = C_i(a)$, on the message m
  - When m is received by b in Pj, Pj sets $C_j$ to be the maximum value of $C_j + d$ or $T_m + d$ for some increment d

Definition of precede

- Def: Event a in Pi precedes event b in Pj if and only if (system-wide)
  1. $C_i(a) < C_j(b)$ OR 2. $C_i(a) = C_j(b)$ and $Pi < Pj$
- Assume that each process Pi is ordered by a unique value of i
- This relation is written as $a \rightarrow b$

Example

```
<table>
<thead>
<tr>
<th>P1</th>
<th>P2</th>
<th>P3</th>
</tr>
</thead>
<tbody>
<tr>
<td>e1</td>
<td>e2</td>
<td>e3</td>
</tr>
<tr>
<td>e4</td>
<td>e5</td>
<td>e6</td>
</tr>
<tr>
<td>e8</td>
<td>e7</td>
<td></td>
</tr>
</tbody>
</table>
```

A partial ordering

```
e1 \rightarrow e4 \rightarrow e7 (P1)
e1 \rightarrow e3 (m)
e5 \rightarrow e8 (m)
e5 \rightarrow e8 (why?)
```

Example

```
<table>
<thead>
<tr>
<th>P1</th>
<th>P2</th>
<th>P3</th>
</tr>
</thead>
<tbody>
<tr>
<td>e1</td>
<td>e2</td>
<td>e3</td>
</tr>
<tr>
<td>e4</td>
<td>e5</td>
<td>e6</td>
</tr>
<tr>
<td>e8</td>
<td></td>
<td>e7</td>
</tr>
</tbody>
</table>
```

A DAG

```
e1 1.1   1.2   1.3
e2 2.1   2.2   e2
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>e5  3.1   3.2 1.5</td>
<td></td>
</tr>
</tbody>
</table>
|     | e8  3.3   2.3   e6
```

Becomes a total ordering on events
Total Ordering of Events

- Any total ordering on events must be consistent with the existent partial order.
- One solution: a topological sort on the partial order – after the fact.
- Lamport: Uses an event number and a time stamp on all events.
- Further, a timestamp is attached to all messages.

Logical Ordering of Events Using Counters

<table>
<thead>
<tr>
<th>Process 1</th>
<th>Process 2</th>
<th>Process 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Counter</td>
<td>Event</td>
<td>Counter</td>
</tr>
<tr>
<td>1</td>
<td>a</td>
<td>0</td>
</tr>
<tr>
<td>2</td>
<td>b</td>
<td>3</td>
</tr>
</tbody>
</table>

c is the event of receiving b
f is the event of receiving d

Each requires a counter adjustment to preserve the happens-before relationship.

Logical Ordering of Events Using Physical Clocks

<table>
<thead>
<tr>
<th>Process 1</th>
<th>Process 2</th>
<th>Process 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Physical clock</td>
<td>Events</td>
<td>Physical clock</td>
</tr>
<tr>
<td>10</td>
<td>a</td>
<td>10</td>
</tr>
<tr>
<td>20</td>
<td>b</td>
<td>29.21</td>
</tr>
</tbody>
</table>

c is the event of receiving b
f is the event of receiving d

Each required a clock adjustment to preserve the happens-before relationship.

Causal Events

- Causal:
  1. Expressing or indicting cause;
  2. Relating to or acting as cause
     - (Merriam-Webster)

- Causal events:
  - If e1 → e2, then C(e1) → C(e2)
  - Two events may have the same timestamp
    - Just include the i of Pi as part of the timestamp.
Definition

- For each process \( p \),
  - Initialize the timestamp, \( p.TS \), to zero
  - On each event,
    - If \( e \) is receipt of message \( m \)
      - \( p.TS = \max(m.TS, p.TS) \);
    - \( p.TS ++ \);
    - \( e.TS = p.TS \);
    - If \( e \) is sending message \( m \)
      - \( m.TS = p.TS \);

Limitation of Lamport’s Clocks

- If \( a \rightarrow b \), then \( C(a) < C(b) \)
- But the reverse is not necessarily true – if the events occur in different processes
  - We can’t tell how \( a \) and \( b \) are related
  - Each clock can independently advance based on its local events
  - We need messages exchanges to synchronize between a pair of processes

Concurrent Events

- There is an arbitrary ordering of concurrent events
- This can lead to a **causality violation**:
  - When distributed objects are mobile, i.e. they can move freely among processes
  - This may happen when load balancing occurs

Casuality Violation
Causality Violation

- Message m₀ arrives late to P₂.
- Message m₃ arrives at P₂ before P₂ knows that T is migrating there.
- To fulfill the transitivity condition, m₃ should have arrived at P₂ after m₀ arrived at P₂.

Notation

- \( s(m) \) = the event of sending message \( m \)
- \( r(m) \) = the event of receiving message \( m \)
- \( m₁ < c m₂ \) if \( s(m₁) \rightarrow s(m₂) \)
- A causality violation happens if \( m₁ < c m₂ \), but \( r(m₂) < p r(m₁) \)
- Need a comparison function \( f \) such that
  - \( e \rightarrow e' \) iff \( f(e) < f(e') \)
  - Idea – vector timestamps

Vector Clocks

- Each \( P_i \) keeps a clock vector \( C_i[k], k=1,\ldots,n \)
- The kth entry is \( P_i \)'s best guess of what process \( P_k \) has for its clock values.
- A message carries a timestamp vector of the clock vector of the sender.
- A receiver updates its clock vector using the timestamp vector from the message.
Vector Clocks

- The vector clocks provide a partial ordering of the timestamps
  - Using a vector comparison (all elements must be =, <, or > pairwise
  - If \( ta < tb \) or \( ta > tb \), then a and b are causally related
  - Otherwise a and b must be concurrent

Causal Ordering of Messages

- For M processes,
  - Initialize \( p.VT = [0, 0, \ldots, 0] \)
  - On event \( e \),
    - If \( e \) is receipt of message \( m \)
      - For \( i=1 \) to \( M \)
        - \( p.VT[i] = \max(p.VT[i], m.VT[i]) \)
    - \( p.VT(self) ++ ; \)
    - \( e.VT = p.VT ; \)
    - If \( e \) is sending message \( m \)
      - \( m.VT = p.VT ; \)

Lamport vs Vector Clock Timestamps

- 4 processes (P1, P2, P3, P4) with events a, b, c, d, e, f, g, ...

Lamport vs Vector Clock Timestamps

- Lamport Timestamps
Lamport vs Vector Clock Timestamps

- Vector Clock Timestamps

References

- http://www.cs.colostate.edu/~cs551/CourseNotes/Synchronization/SynchTOC.html