

# Display & Rendering

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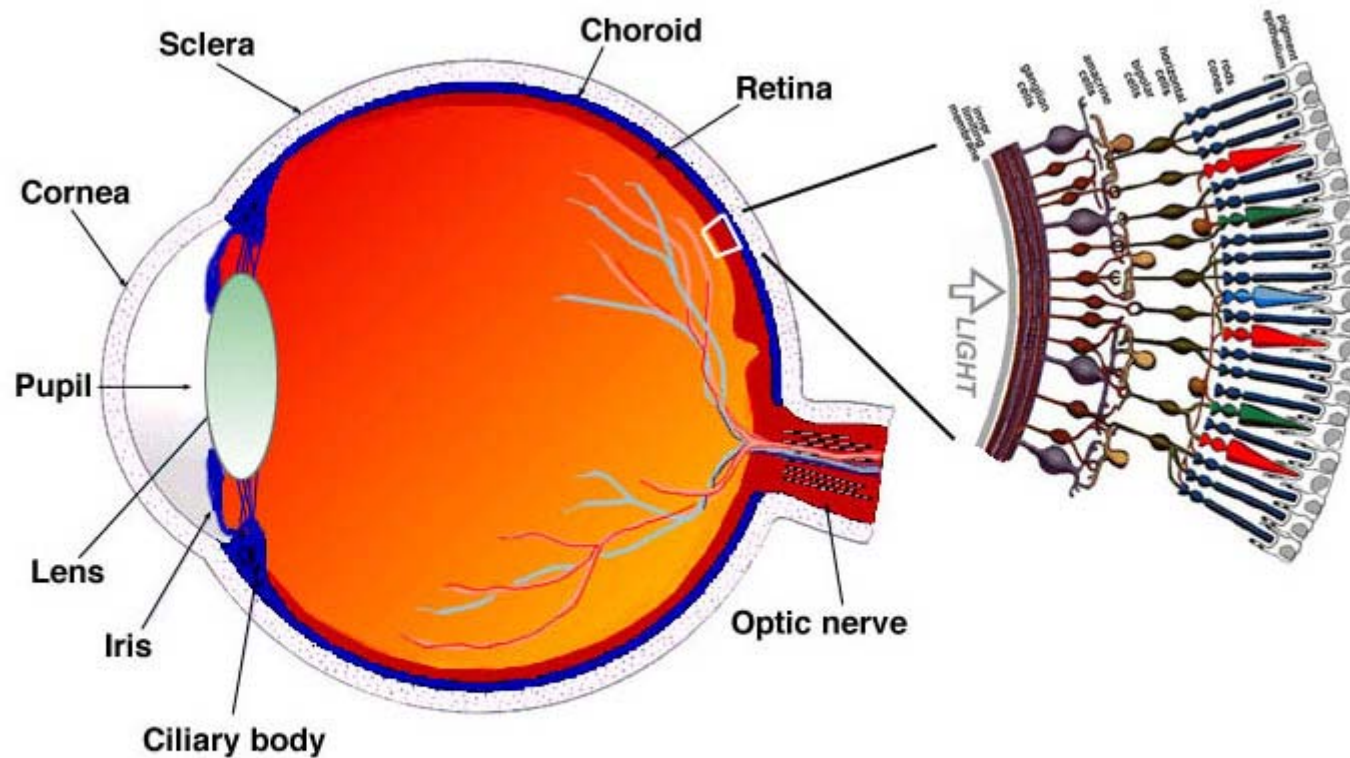
# Human Perception System

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- Obtain information about environment through senses:
  - Vision: primary form of perception in most VR
  - Audition: second most common in VR
  - Haptic/Touch: perceptible on through direct contact
  - Olfaction
  - Gustation
  - Vestibular/kinesthetic sense
- VR systems mimics the senses by output of computer-generated stimuli rather than natural stimuli to one or more of these sense.

# Vision

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**Fig. 1.1. A drawing of a section through the human eye with a schematic enlargement of the retina.**

Image from <http://webvision.med.utah.edu/sretina.html>

# Audition

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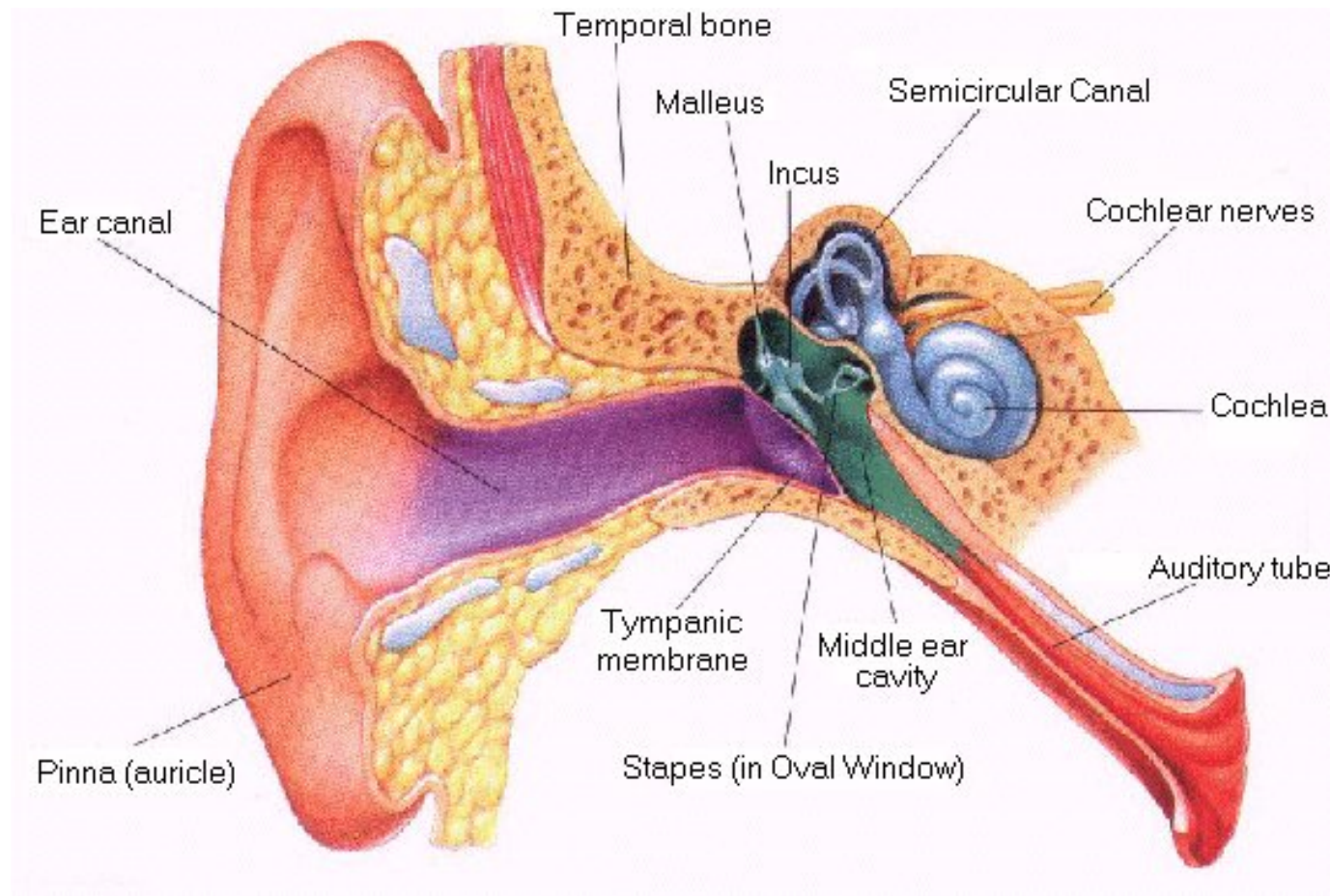


Image from [http://www.infj.ulst.ac.uk/~pnic/HumanEar/Andy's%20Stuff/MScProject/workingcode\\_Local/EarChapter.html](http://www.infj.ulst.ac.uk/~pnic/HumanEar/Andy's%20Stuff/MScProject/workingcode_Local/EarChapter.html)

# Touch

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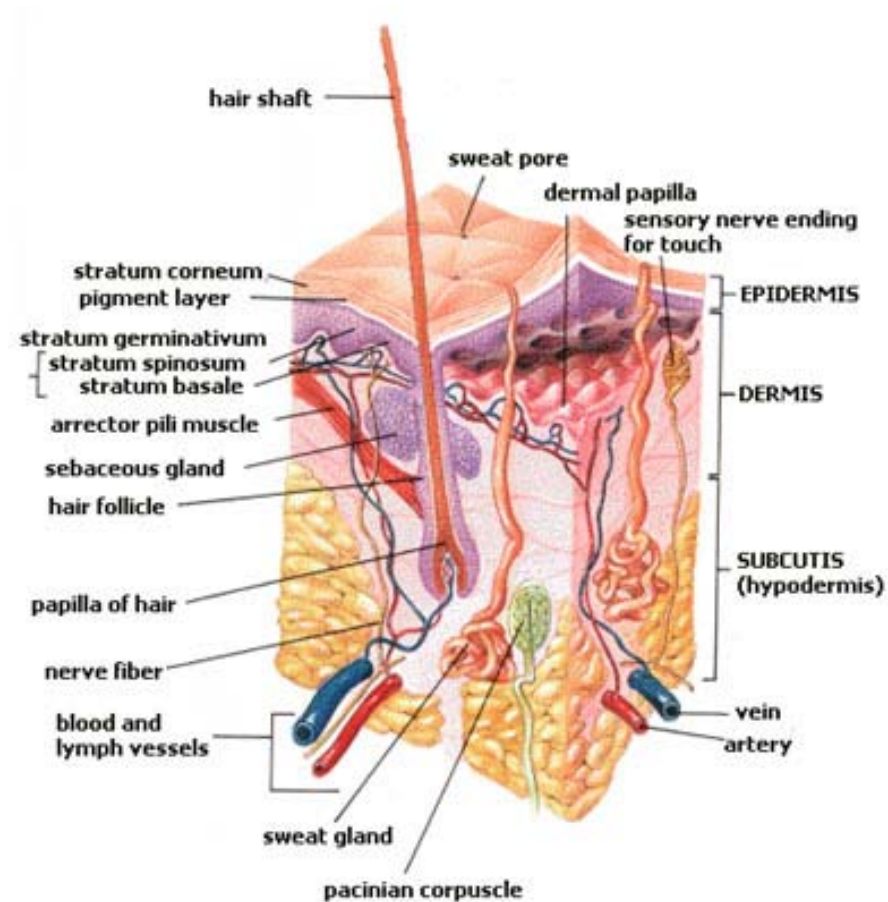


Image from [http://en.wikibooks.org/wiki/Human\\_Physiology/Print\\_Version](http://en.wikibooks.org/wiki/Human_Physiology/Print_Version)

# Olfaction

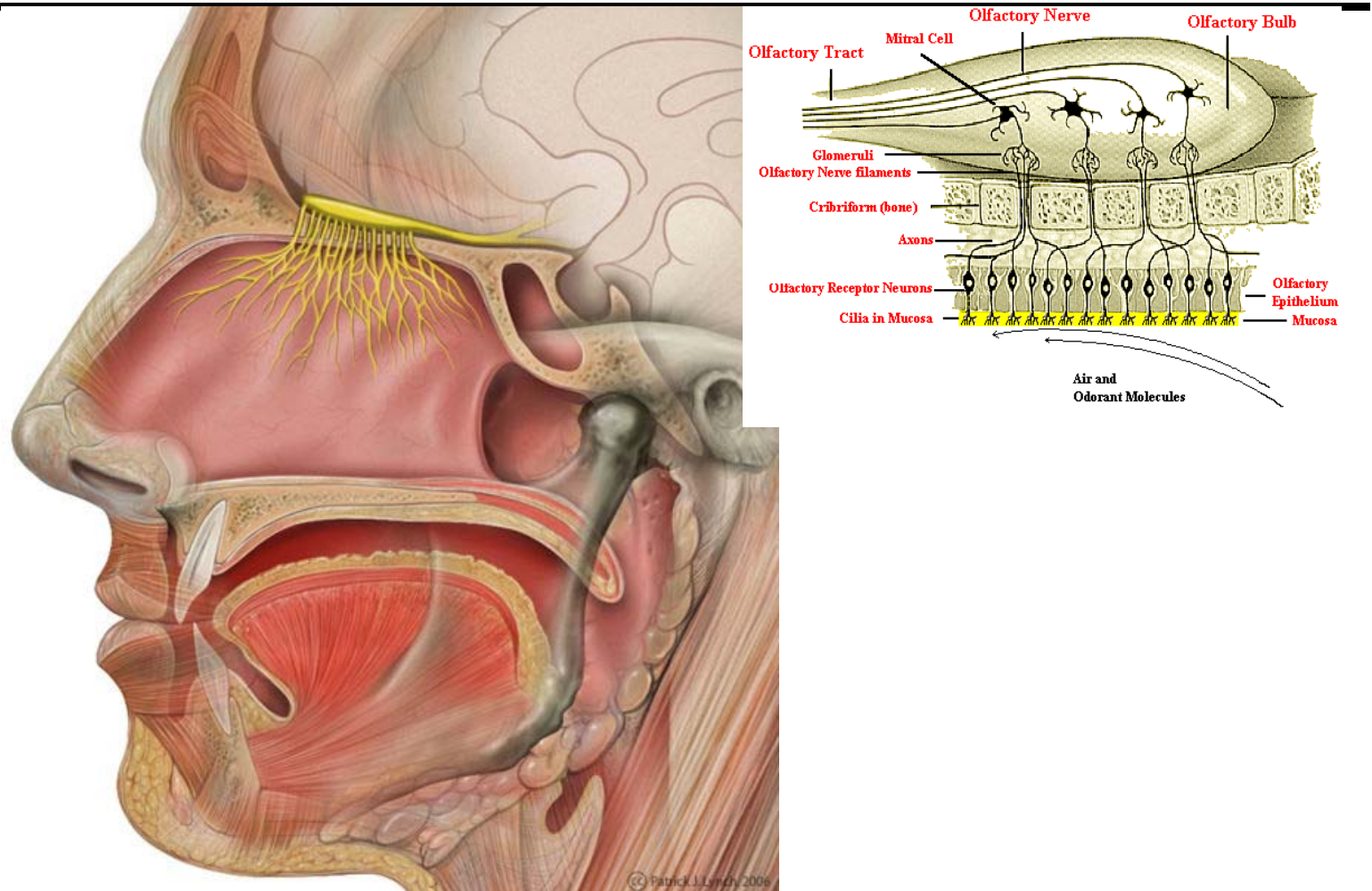


Image from [http://en.wikibooks.org/wiki/Human\\_Physiology/Print\\_Version](http://en.wikibooks.org/wiki/Human_Physiology/Print_Version)

# Gustation

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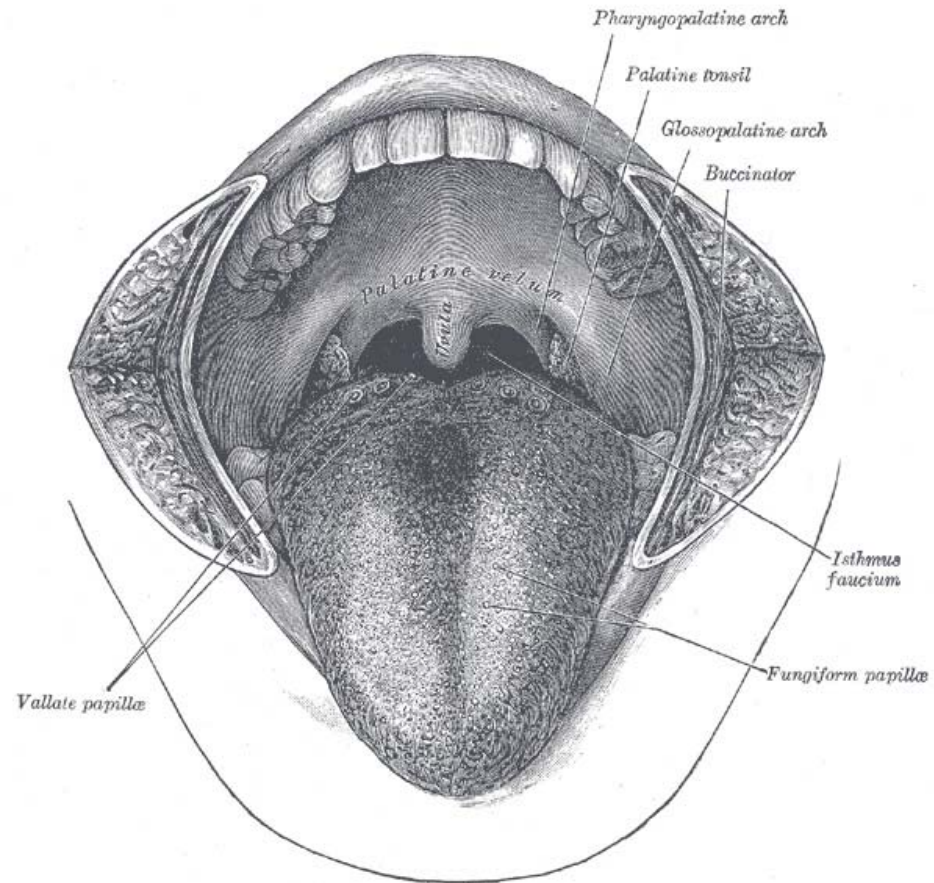


Image from [http://en.wikibooks.org/wiki/Human\\_Physiology/Print\\_Version](http://en.wikibooks.org/wiki/Human_Physiology/Print_Version)

# Visual Displays

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- ❑ Fishtank VR stationary display
- ❑ Projection VR stationary display
  - Surround-screen displays
  - Tabletop displays
  - Wall displays
- ❑ Occlusive head-based display
  - Head-mounted display (HMD)
  - Binocular mono-oriented monitor (BOOM)
- ❑ Nonocclusive head-based display
- ❑ Hand-coupled display

# Visual Display Presentation Qualities

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## □ Color

- mostly trichromatic color
- monochromatic color in some displays – e.g. see-through HMD
- field-sequential color display – overlays the three colors in same location

## □ Spatial resolution

- number of pixels
- pixel density

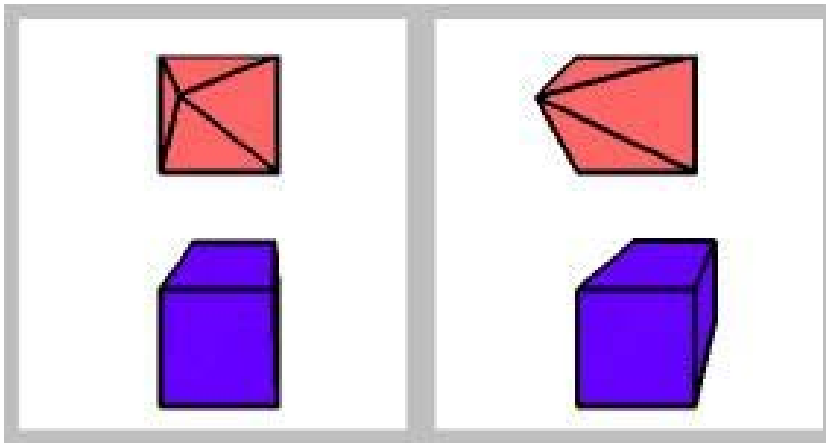
## □ Contrast/Brightness

- dynamic range of the display
- LCD displays tend to have lower contrast than CRTs
- See-through HMD requires brighter display

# Visual Display Presentation Qualities

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- Number of display channels
  - two for stereoscopic displays
  - sometimes two display channels, but the same image on both
  - many ways to transmit multiple channels: color (anaglyph), polarization, time-multiplexing, spatial-multiplexing
  - can combine techniques to introduce more channels (perhaps for two viewers) – e.g. Fakespace DuoView



# Visual Display Presentation Qualities

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## □ Focal distance

- distance at which images seem to appear
- typically the screen in stationary displays
- can be infinite via optics in an head-based display

## □ Opacity

- occlude the real world or not
- CAVE does not occlude the real world
- most HMDs occlude the real world
- see-through HMD is generally used for AR applications

## □ Masking

- hiding things behind an object
- a problem when a virtual object comes between the viewer's eyes and a physical object
- physical objects (e.g. user hand) mask virtual objects in stationary displays

# Visual Display Presentation Qualities

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## □ Field of view

- measure of the angular width of user's vision
- typical HMDs cover about 100 degree FOV with about 60 degree stereo overlap FOV

## □ Field of regard

- amount surrounding space where virtual world is displayed
- HMDs are typically 100%
- CAVEs are often much less (except for 6-sided CAVEs)

## □ Head position information

- typically position trackers monitor six degree of freedom (DOF) of the participant's head
- 3-DOF orientation is needed for HMDs
- 3-DOF location is needed for stationary displays

# Visual Display Presentation Qualities

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- ❑ Graphics latency
  - lag between user movements and the update of the display
  - source of causing nausea or headaches
  - lag is very noticable when rotating head in HMD
  - lag is less noticable when rotating head in CAVE
- ❑ Temporal resolution (frame rate)
  - image updates per second (measured as FPS or Hz)
  - motion pictures capture 24 FPS
  - 15 Hz is considered marginally acceptable
  - 10 Hz and below causes brain to notice that it is seeing a series of still images

# Logical Qualities of Visual Displays

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## □ User mobility

- can effect on mental immersiveness and usefulness of user VR experience
- e.g. cables that tether the user, tracking systems with limited range, or screens that prevent further physical movement

## □ Interface with tracker methods

- type of displays can influence the selection of tracking methods

## □ Environment requirements

- conditions of the surrounding space necessary to provide a good VR experience
- projection-based displays require low light
- CAVE requires big rooms

# Logical Qualities of Visual Displays

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- ❑ Associability with other sense displays
  - headphones and HMDs work well together
- ❑ Portability
  - large stationary displays are not portable
  - e.g. HMD vs. CAVE



# Logical Qualities of Visual Displays

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- ❑ Throughput
  - HMDs often requires a minute or two to change viewers
  - easier for people to enter and exit a CAVE
- ❑ Encumbrance
  - generally more wires associated with HMDs
- ❑ Safety
  - eye fatigue and nausea can result from poor optics
  - can't see what you're doing in real world in an occlusive HMDs
- ❑ Cost
  - generally head-based displays tend to be lower priced than large-screen projection systems
  - CAVE requires more graphics power

# Monitor-based or Fishtank VR

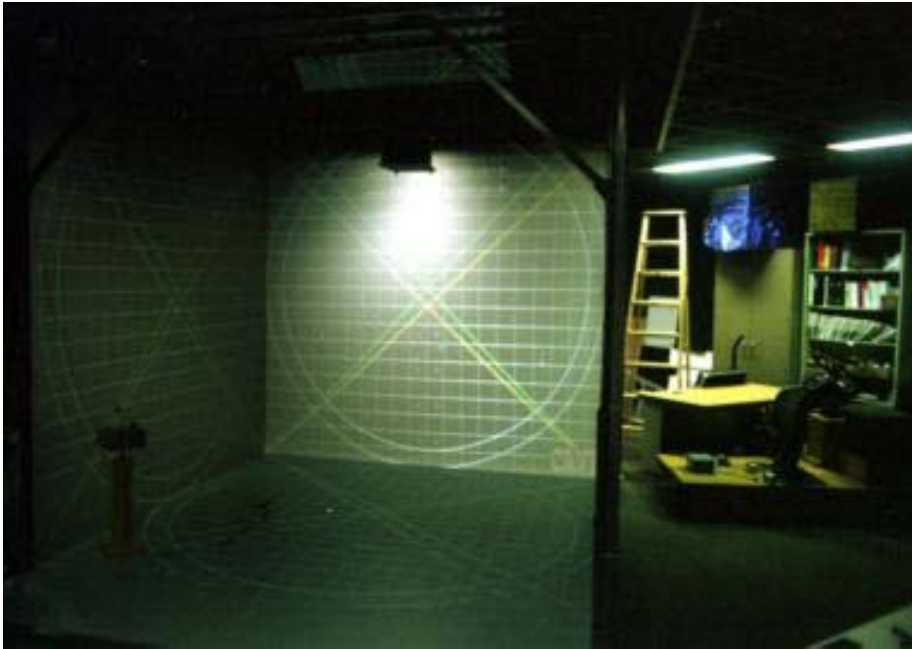
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- ❑ Use standard computer monitor
- ❑ Differ from generic interactive 3D graphics displayed on a monitor because render scenes based on the user's head tracking data
- ❑ Fewer components & lower cost
- ❑ Standard interface devices available (keyboard, mouse)
- ❑ Limited FOV & FOR
- ❑ Generally less mentally immersive

# Projection-based VR: Surround-screen displays

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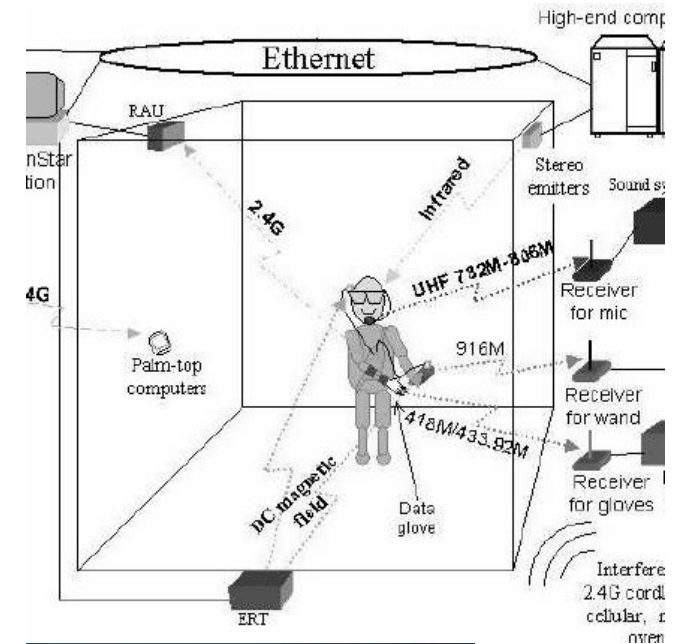


- ❑ Mostly rear-projected to avoid the participants casting shadows on the screen
- ❑ Larger more costly displays
- ❑ Longer range tracking systems
- ❑ Greater FOV & FOR
- ❑ Not isolated from the real world
- ❑ Multi-viewers friendly
- ❑ Not very encumbering
- ❑ Less eye strain
- ❑ More space required
- ❑ More graphics power required
- ❑ Occlusion problem

# Projection-based VR: 6-sided CAVE

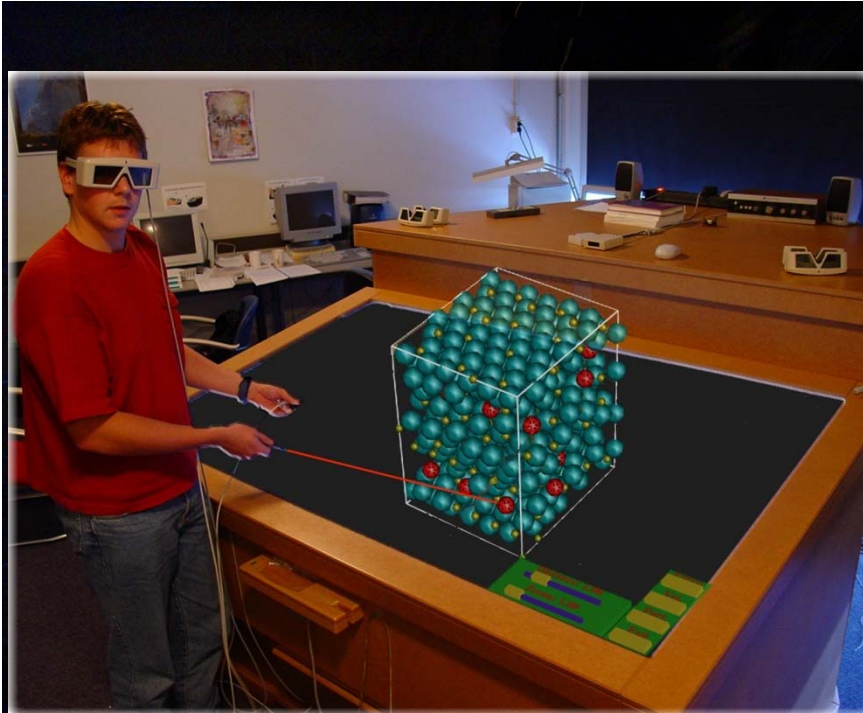


[https://www.mechdyne.com/case\\_study/iowa-state-university/](https://www.mechdyne.com/case_study/iowa-state-university/)



# Projection-based VR: Tabletop displays

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- ❑ Good for direct manipulation
- ❑ Good for god's eye view
- ❑ Good for changing orientation
- ❑ Less immersion than surrounded VR displays

# Projection-based VR: Wall displays

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- ❑ 3D movie-like VR displays
- ❑ Larger tiled or curved wall displays are suited for larger audiences – larger pixel, need more projectors
- ❑ Less immersion than surrounded VR displays
- ❑ Problem of seamless integration

# Head-based Displays

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- ❑ Small, lightweight screens
- ❑ More portable than stationary VR displays
- ❑ More encumbering than stationary VR displays
- ❑ Tethering to computer
- ❑ 100% FOR
- ❑ Limited FOV
- ❑ No peripheral vision
- ❑ Lag in tracking is detrimental
- ❑ Eye fatigue

# Head-Mounted Displays (HMD)

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- ❑ e.g. Sony Glasstron
- ❑ HMD Vendors at <http://www.faqs.org/faqs/virtual-worlds/visual-faq/section-2.html>



# Best VR headset for 2020

Oculus Quest, HTC Vive or PSVR? It all depends on who you are and how much you want to spend.



Scott Stein  Sept. 8, 2020 7:38 a.m. PT



## Oculus Quest

The best standalone VR

[Jump to details](#)

**\$632 AT AMAZON**



## Sony PlayStation VR

Still worth it for the games

[Jump to details](#)

**\$245 AT AMAZON**



## Oculus Rift S

Best easy-to-set-up PC VR

[Jump to details](#)

**\$399 AT LENOVO**



## Valve Index

Best PC VR to explore the future of VR controllers

[Jump to details](#)

**\$999 AT STEAM**



## HTC Vive Cosmos

Could be a flexible, modular system

[Jump to details](#)

**\$700 AT AMAZON**

Yes, VR is still around, and standalone VR devices have seen a huge spike in interest this year since the March release of Valve's [Half-Life: Alyx](#). But this technology is ever-evolving, and the concept of a VR device in 2020 is in transition. This is because companies such as Qualcomm (which makes the chips inside most self-contained VR headsets, including the popular [Oculus Quest](#)) are [building new chips](#) that point to a wave of [better standalone headsets](#) at lower prices -- including ones that plug into your phone.

Meanwhile, older mobile VR or phone-based VR headsets, like the [Samsung Gear VR](#) and Google Daydream are basically dead. A good number of the current iPhone,

<https://www.cnet.com/news/best-vr-headset-for-2020/>

# See-thru Head-based Displays

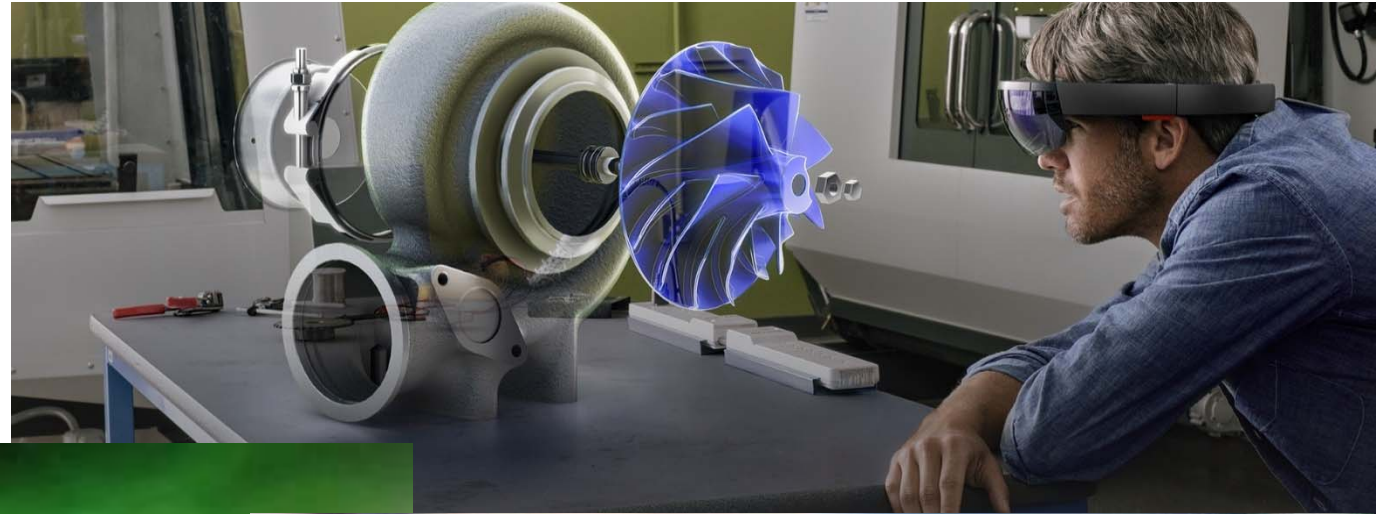
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- ❑ Optical see-through vs. video see-through
- ❑ Require 6-DOF tracking
- ❑ Registration of tracking with the real world
- ❑ Application must live within the restriction of the real world
- ❑ Proper rendering of object occlusion is difficult

# See-thru Head-based Displays

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# Handheld VR

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- ❑ Limited example of handheld VR – e.g. Chameleon, Virtual binoculars
- ❑ Used as a magic lens
- ❑ Need to track both the screen and the head
- ❑ Registration of tracking with the real world
- ❑ Can be used in conjunction with projection-based VR displays

# Auditory Displays

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- ▣ Speakers
- ▣ Headphones

# Aural Display Presentation Qualities

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- ❑ Number of display channels
  - monophonic
  - stereophonic
  - quadraphonic, octaphonic, 5.1
  - multiple speakers rely on ears to naturally localize sounds
- ❑ Sound stage
  - source from which a sound appears to emanate
  - **head-referenced** vs. **world-referenced**
    - ❑ head-referenced sound stage moves with the head
    - ❑ world-referenced sound stage remains fixed with the world
  - sounds require filtering based on head tracking to reproduce a world-referenced sound stage with headphones

# Aural Display Presentation Qualities

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## □ Localization (Spatialization)

- localization is human brain's ability to determine the location from which a sound is emanating
- spatialization is technology's ability to make a sound appear to come from particular points in space
- spatialization is easier with headphones due to direct sound control

## □ Masking

- loud sounds mask softer sounds
- physical objects can mask a sound
- closed headphones are best for VR experience where the participants is only supposed to hear sounds from the virtual world

## □ Amplification

- Need to boost the sounds to hearable levels

# Logical Qualities of Aural Displays

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- ❑ Noise Pollution
  - speakers require quiet and echo free environment
- ❑ User mobility
  - wired headphones limit mobility
- ❑ Interface with tracker
  - magnets in the speaker/headphones
- ❑ Environment requirements
- ❑ Associability with other sensors
  - typically stationary with stationary, head-based with head-based
- ❑ Portability & Encumbrance
  - speakers generally more comfortable for longer use
- ❑ Throughput
  - speakers work better for larger audiences
- ❑ Safety & Cost

# Simple Virtual Environment Audio

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- Intensity fall-off
- Headphones also block real-world noises
- Ambient sound in the background
- Subwoofer in seat or platform
- Present speech instead of text

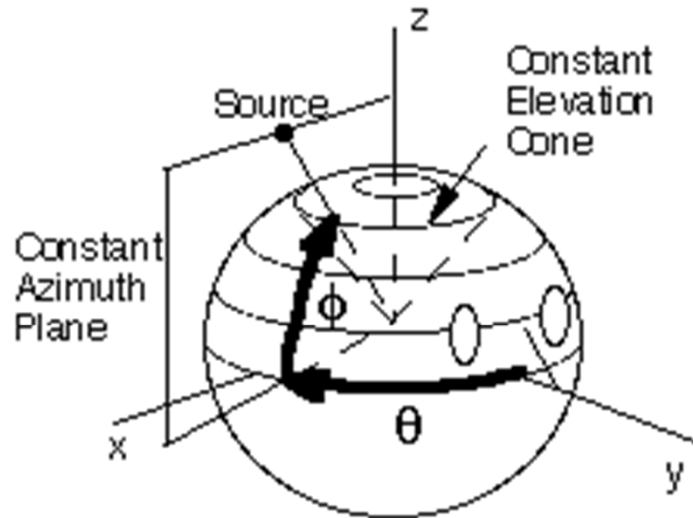
# 3D Sound Localization

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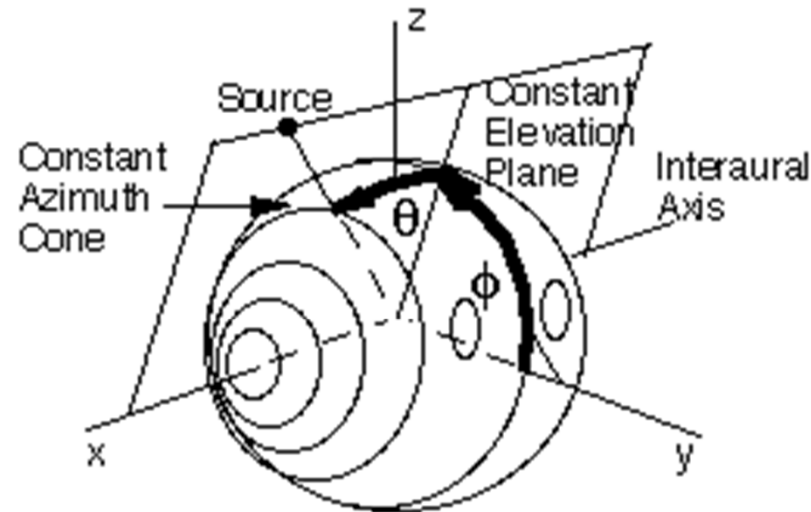
- Spatialization
- Works well in plane of ears
- Based on:
  - Interaural intensity differences (IID)
  - Interaural time differences (ITD)
- Head-Related Transfer Function (HRTF)

# Vertical-Polar Coordinate System

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Vertical-Polar Coordinates



Interaural-Polar Coordinates

$\theta$ : azimuth (angle between the nose and a plane containing the source and the vertical axis  $z$ )

$\phi$ : elevation (angle between the horizontal plane by a line passing through the source and the center of the head)

$\rho$ : range (distance to the source measured along this line)

# Azimuth Cues

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## □ Interaural time difference (ITD)

- difference in the arrival time of the sound at the two ears
- ITD is zero when the azimuth angle is 0 degree, i.e. the source is directly in front of or directly behind the head
- $ITD = (a/c)(\theta + \sin \theta)$ 
  - $a$ : the head radius
  - $c$ : the speed of sound ( $\sim 343$  m/s)
  - $\theta$ : source azimuth

## □ Interaural intensity differences (IID)

- difference in the intensity of sound reaching the ears
- the closer ear hears a sound with higher intensity
- detectable for sounds with high frequencies ( $> 1.5$  kHz)
- for low frequency, ITD dominates

# Elevation Cues

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## □ Different reflections

- Due to the asymmetry of the outer ear, especially the pinna
- the path difference between the direct and pinna-reflected sound changes with the elevation angle
- sound coming from a source located above the user's head has quite a different reflection path than sound coming from a source in front of the user

## □ Different amplification (and attenuation)

- by interference between reflected sounds
- some frequencies are amplified and others are attenuated

## □ Pinna provides the primary cue for source elevation

- user's face and shoulders geometry also influences the way the sound is reflected towards the outer ear

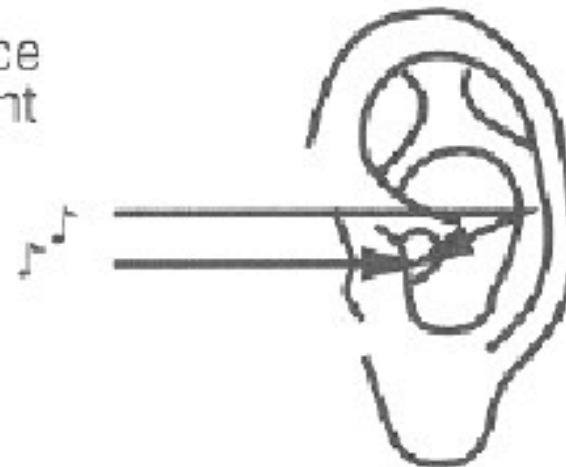
# Elevation Cues

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Source  
above



Source  
in front



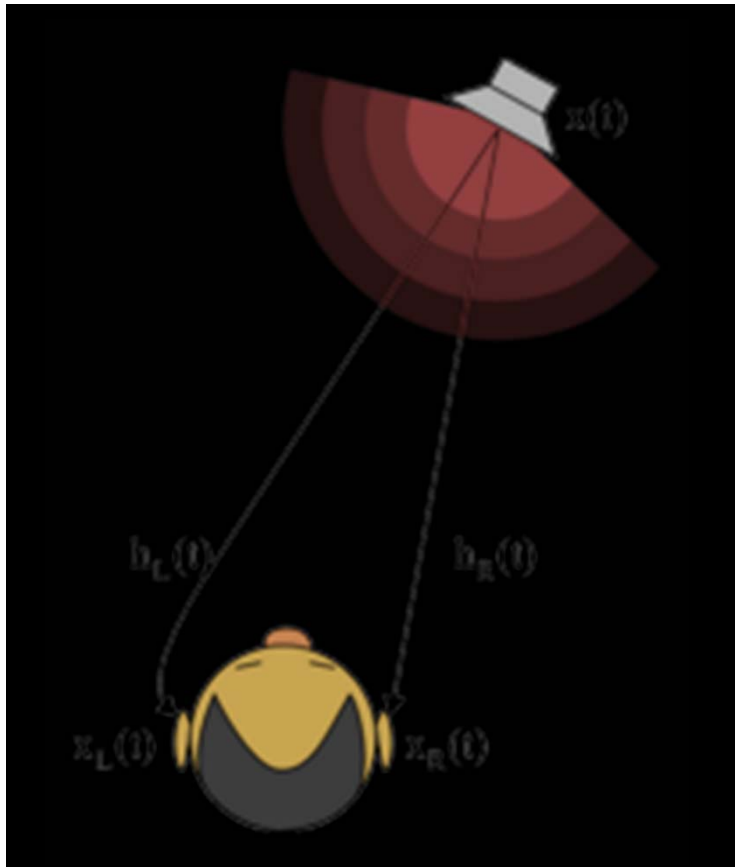
# Range Cues

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- Perceived loudness
  - prior knowledge of a given sound source
  - faint siren (which is a normally high-energy sound source) is perceived as being distant
  - clear whisper (which is a normally faint sound source) is perceived as being close
- Motion parallax
  - change in sound source azimuth when the user is moving
  - large motion parallax indicates a source nearby
- Ratio between direct and reflected sound
  - energy of the direct sound drops off with the square of the source range
  - energy of the reflected sound does not change much with range

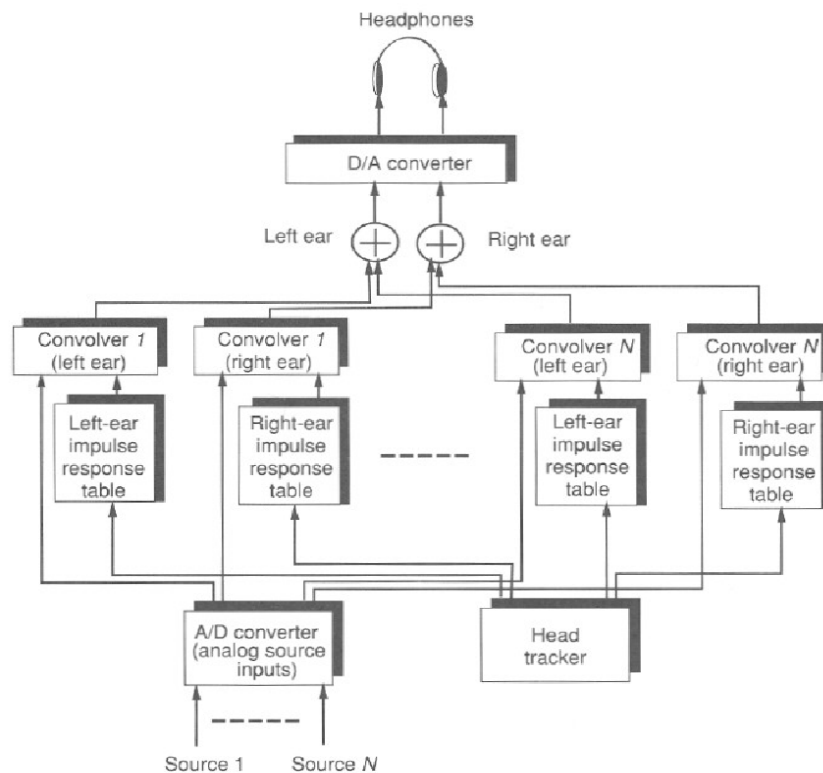
# Head-Related Transfer Functions

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- HRTF captures all of the physical cues to source localization
- Experimental measurement of transfer function
  - sounds from speakers at different locations
  - tiny microphones in the ears
  - analysis of recordings from both ears
  - head-related impulse responses (HRIRs)
  - head-related transfer functions (HRTFs)
- Each individual has his/her HRTF signature, also called ear print

# Convolvotron



- ❑ Crystal River Engineering
- ❑ HRTF-based spatial audio system
- ❑ The system can be customized for a particular individual by measuring and using that person's HRTF
- ❑ Echoes and room reverberation can be added by including a room simulation model
- ❑ Head motion can be accounted for by combining the absolute location of the source with the outputs of a head tracker to select the appropriate HRTFs

# Ambisonics

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- ▣ Presentation of 3D spatialized sound using multiple stationary speakers
- ▣ surrounding sound recording, synthesis and playback system

<http://en.wikipedia.org/wiki/Ambisonics>

# Haptic Displays

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- Kinesthetic/Force displays
- Tactile displays
- End-effector displays
- Robotically operated shape displays

# Haptic Display Presentation Qualities

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## □ Kinesthetic cues

- nerve inputs that sense angles of joints, muscle length, tension, and resistance to muscle effort (force) within the body
- helps us determine firmness, approximate shape, and physical force

## □ Tactile cues

- sensory receptors at the skin
- mechanoreceptor – shape and surface texture
- thermoreceptor – heat
- electroreceptor – electric current flow
- nociceptor – pain

## □ Grounding

- force/resistance displays require an anchor
- self-grounded vs. world-grounded

# Haptic Display Presentation Qualities

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- Number of display channel
  - how many points of contact with the body
  - 1 channel when Phantom has one point where the user can influence the virtual world
- Degrees of freedom
  - 6-DOF in unconstrained movement
  - 1-DOF display for how far can the thumb be opened/closed
  - 1-DOF display for how far down a tube can you insert a laparoscope camera
  - 2-DOF display for how far down a tube, plus twist
  - 3-DOF display for down, twist, clamping action and resistance
  - 3-DOF display for location of the finger or stylus
  - 6-DOF display for location and orientation

# Haptic Display Presentation Qualities

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## □ Form

- the shape of the physical unit with which the user interacts
- generic form, such as stick, ball, or plane
- specific object, such as handgun, or steering wheel
- amorphous that changes shape to multiple specific representations

## □ Fidelity

- how rapidly the system can change to the proper display (force, temperature)
- can be rated by a maximum stiffness measurement taken in Newtons/meter (Nt/m)
- a stiffness of 20 Nt/cm as a solid immovable wall
- 40 Nt/cm is the maximum force that a human finger can exert
- 10 Nt/cm is the highest force used when doing fine manipulation

# Haptic Display Presentation Qualities

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- Spatial resolution
  - higher resolution required at the fingertip
  - fingertips can sense difference 2mm apart
  - 30 mm on the forearm & 70 mm on the back
- Temporal resolution
  - how quickly the system can be updated to new display
  - low frame rate on a force display causes the object to be perceived as shakey
  - 1000 Hz is a good minimum
- Latency tolerance
  - low latency display is crucial, especially for force display
- Size
  - larger displays allow broader range of motion

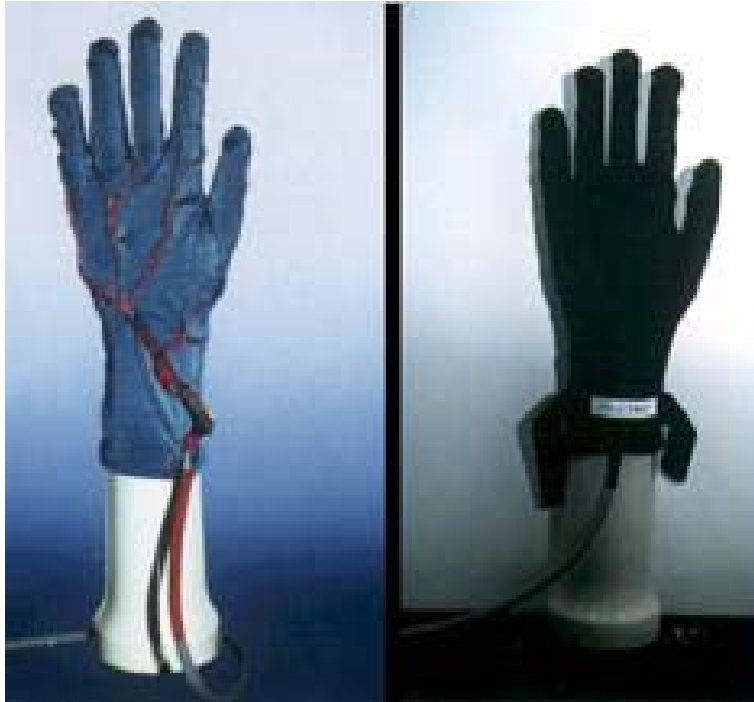
# Logical Qualities of Haptic Displays

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- User mobility
  - world-grounded displays require the user to be near the device
- Interface with tracker
  - responsive and accurate tracking system is required
- Environment requirements
- Associability with other sense displays
  - occlusive HMDs often are used in conjunction with haptic displays
- Portability
- Throughput
- Encumbrance
  - self-grounded, exoskeleton-style devices are generally much encumbering
- Safety
  - safety is a significant concern with many haptic displays

# Tactile Displays

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Teletact Glove

- Sensed by the skin – the largest single organ of the human body
- Actuators mounted generally on the fingers and hand
- Generally no need for world grounding
- Bladder actuators
- Vibrator actuators
- Pin actuators
- Thermo actuators
- Helps in the fine manipulation of virtual objects
- Less expensive & portable

# Tactile Displays using Vibrators

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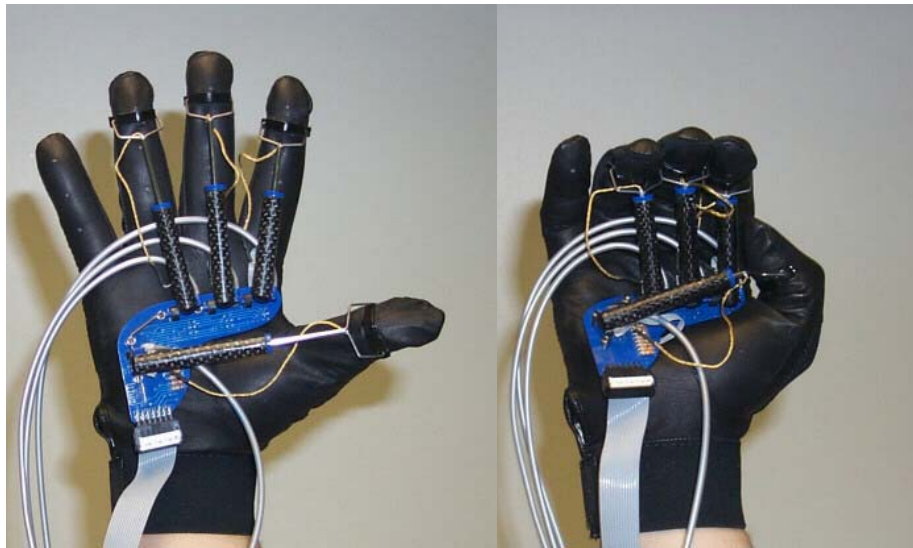
Cyberglove



Cricket Prob

# End-effector Displays

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Rutgers Dextrous Master

- ❑ A mechanical device that provides a force to the participant's extremities
- ❑ Generally linked to mechanical tracking sensors
- ❑ Generally world grounded (exoskeleton method is body-grounded)
- ❑ Often operate with respect to a single point in the virtual world
- ❑ Fast and accurate tracking is usually built into display

# Robotically Operated Shape Displays

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Cybernetic Systems

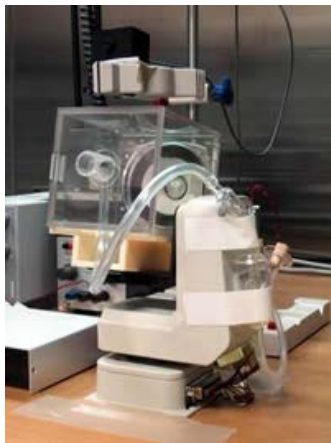
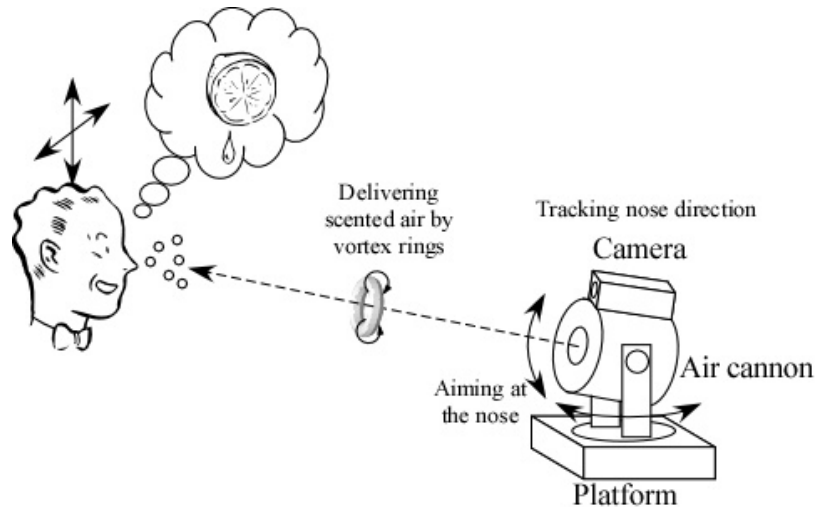
- ❑ Use robots to place a representation of the virtual world where the user is reaching
- ❑ May be generic (corners and edges) – e.g. Cybernetic Systems
- ❑ May be specific (selection of switches) – e.g. Boeing
- ❑ Usually uses a finger surrogate for fast tracking
- ❑ Can provide a very realistic haptic display
- ❑ World-grounded display
- ❑ Works with HMDs

# Olfactory Displays

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- ❑ Very little research is done in olfaction
- ❑ Lack of effective displays and difficulty in producing broad range of stimuli
- ❑ Olfactory events (odor sources) may be near or far, but directional sensitivity is generally poor
- ❑ Temporal sensitivity is poor and response times are slow
  - May need 20-60 seconds between stimuli to resolve different smells
  - To control over stimulus decay rate (without significant air circulation)
- ❑ Smell synthesis
- ❑ Require chemicals
- ❑ Olfactometer
- ❑ Smell-O-Vision

# Olfactory Displays



## ■ ATR Scent Projector

- Projection-based olfactory display with nose tracking
- Unencumbering: Users do not need to wear any devices or glasses
- Localized: Scent can be perceived only within a limited range of space at a certain time
- Composed of "air cannon", scene generator (aroma diffuser), 2DOF platform and a CCD camera

Image from <http://www.mis.atr.jp/past/sem/scent.html>

# Olfactory Displays



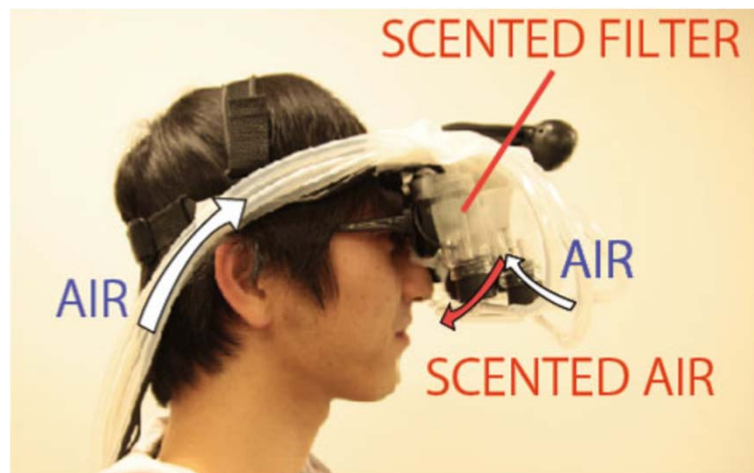
- ❑ Wearable Olfactory Display by U. of Tokyo
  - odor-generating unit (air-pump & odor filters)
  - odor-controlling unit (a notebook PC and a device controller)
  - odor-presenting unit (to present the mixing of odor air)

# Olfactory Displays

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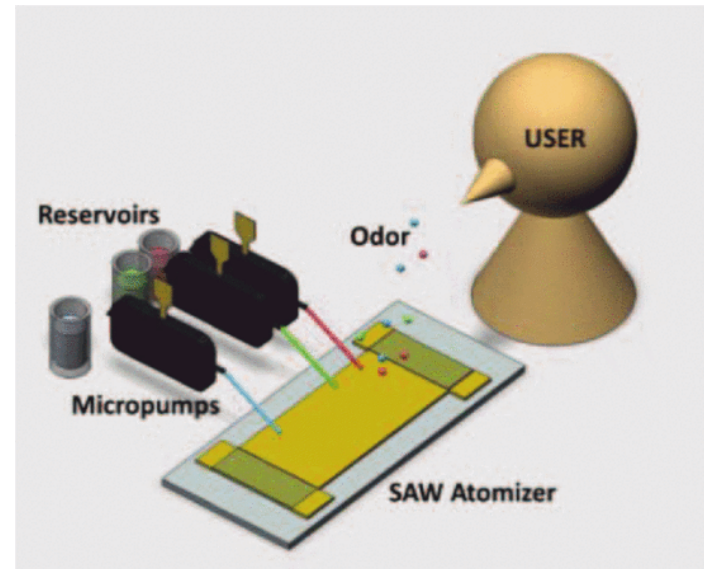
- Meta Cookie @ University of Tokyo – Air-pump type head-mounted olfactory display (2011)



<https://www.exploratorium.edu/blogs/fabricated-realities/meta-cookie-olfactory-gustatory-augmented-reality>

# Olfactory Displays

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VR Oculus Rift Olfactory Display @ Tokyo Institute of Technology (2016)  
<https://hackaday.com/2017/03/21/your-vr-doesnt-stink-yet/>  
<https://www.youtube.com/watch?v=LCYe4eul3TA>

# Gustatory Displays

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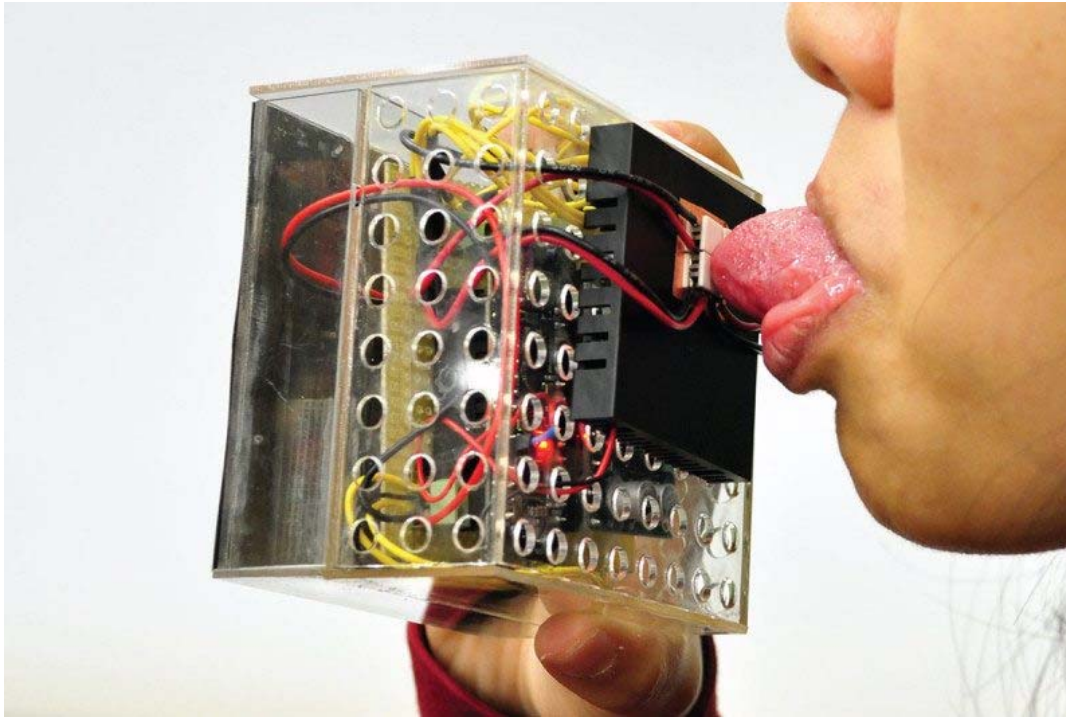
- ❑ Affected by other senses – strong influence of smell on taste
- ❑ Need more than flavor – e.g. texture
- ❑ Basic elements of taste – salt, sour, bitter, sweet, umami, smell

Food Simulator 2003

Image from <http://www.siggraph.org/s2003/conference/etech/food.html>

# Gustatory Displays

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Unreal: this tastes delicious (2016)

[https://www.newscientist.com/article/](https://www.newscientist.com/article/2111371-face-electrodes-let-you-taste-and-chew-in-virtual-reality/)

[2111371-face-electrodes-let-you-taste-and-chew-in-virtual-reality/](https://www.newscientist.com/article/2111371-face-electrodes-let-you-taste-and-chew-in-virtual-reality/)

# Vestibular Displays

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- ❑ Physically move the user – e.g. motion platform
- ❑ Sense of body movements or acceleration
- ❑ Vestibular information works together with visual and kinesthetic information
- ❑ Virtual body representation
- ❑ Can “display” to these senses by stimulating the proper parts of the brain

# Rendering Systems

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- Visual
- Aural
- Haptic

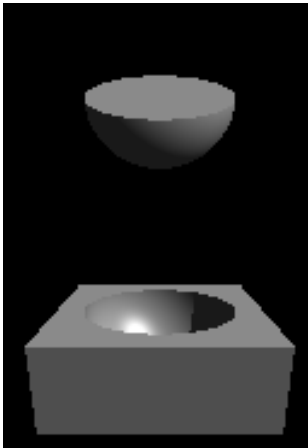
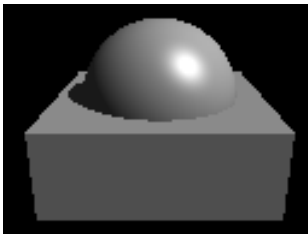
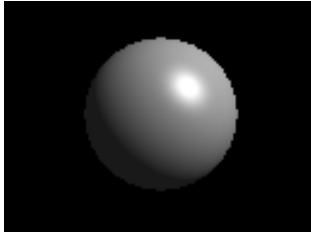
# Visual Rendering Systems

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- Computer graphics
  - generating visual imagery
- Software rendering
  - graphical rendering routines
- Object presentation schemes
  - Geometrically based (polygons, NURBS, CSG)
  - Non-geometric forms (volumetric rendering, particle systems)

# Geometrically-based Representations

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CSG

- ❑ Polygons
- ❑ Constructive Solid Geometry (CSG)
- ❑ Non-Uniform Rational B-Splines (NURBS)
- ❑ Other representations are often converted to polygons for hardware rendering

# Non-geometrically-based Representations

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- ▣ Volume rendering
- ▣ Particle systems



# Techniques for rendering complex visual scenes

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- ❑ Shading
- ❑ Reducing polygons:
  - Texture mapping
  - View culling
  - Level of Detail (LOD)
  - Atmospheric effect, e.g., fog
- ❑ Multiplexing multiple renderers to one screen:
  - Added cost of additional rendering systems
  - Decrease average image latency for each frame
  - Does not decrease onset latency
  - Reduces the maximum delay between the input and the response

# Internal Computer Representation

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- ❑ Most hardware graphics rendering engines are optimized for polygonal representation
- ❑ 3D models created by a model package, Alias, SoftImage, AutoCAD, VRML
- ❑ A scene graph is a mathematical graph that allows objects and object properties (colors, materials, textures) to be related to one another in a hierarchical fashion.

# Aural Rendering Systems

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## □ Sampling

- A common way of producing sounds
- Playback of digitally recorded samples of physical world sounds
- 8 KHz telephone, 44 KHz CD, 96 KHz DVD quality

## □ Sound synthesis

- Spectral method using sound wave's frequency spectrum
- Physical model using physics of the object generating sound
- Abstract synthesis is to create sound using some numerical system

# Techniques for Rendering Complex Sounds

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- ❑ Frequency modulation (FM)
- ❑ Algorithmic additive and subtractive techniques
- ❑ Granular synthesis
  - Combining the sound of a single drop of water falling to produce the sound of a waterfall
- ❑ Sonic effects
  - Convolution – making a sound appear to come from a particular location
  - Reverberation – using reflections of the sound
  - Chorusing – mixing sounds

# Haptic Rendering Systems

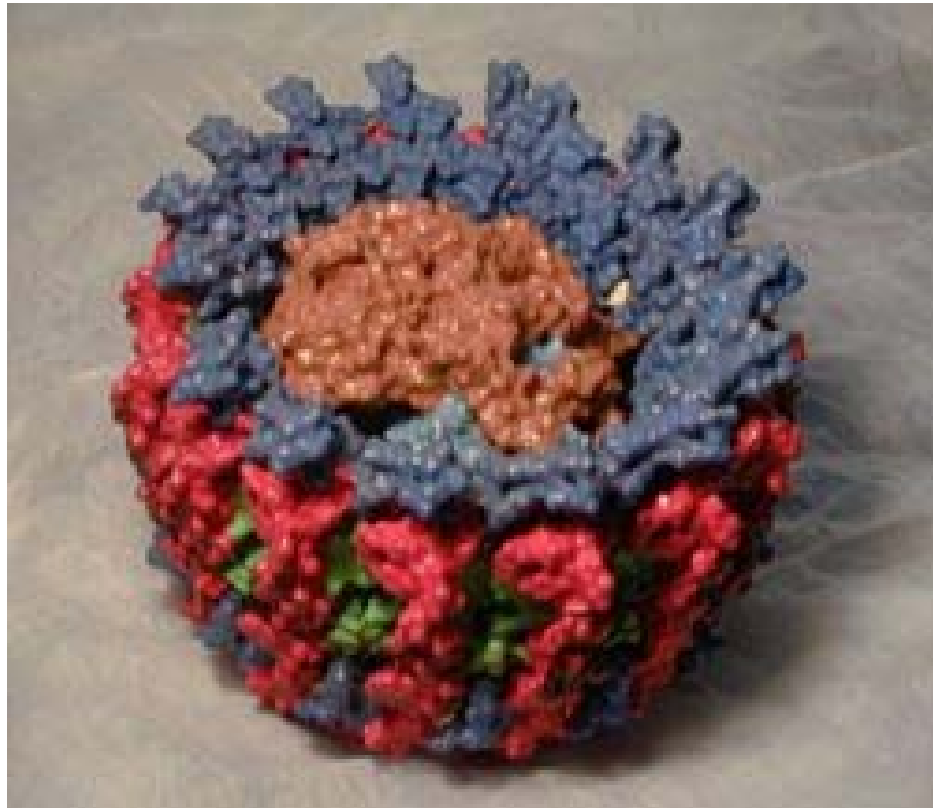
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- ❑ Thermal rendering – usually used on Peltier thermoelectric coolers
- ❑ Pin-based rendering
- ❑ Kinesthetic rendering using force display
- ❑ Robotically operated shape display
- ❑ Physical object rendering – 3D hardcopy, aka stereolithography

# Stereolithography

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<http://en.wikipedia.org/wiki/Stereolithography>

# Techniques for rendering complex haptic scenes with force displays

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Laparoscopic surgery interface

- ❑ Single point of contact with an object
  - E.g. to a fingertip or tip of a stylus
  - Required 3-DOF force display
- ❑ Single point of contact with torque
  - Required 6-DOF force display
- ❑ Constraint of movement
  - E.g. laparoscopic
- ❑ Two points of contact (pinching)
- ❑ Multiple points of contact (grasping)

# Haptic Rendering Techniques

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- Spring and dashpot
  - controls direction, tension, and damping
- Point and plane & Multiple plane
  - interaction between a probe stylus and a surface by placing a virtual planer surface tangential to the probe's tip
- Point to point
- Multi-springs
  - adds torque to any of the other haptic representations
- Inertial and resistant effects
  - resistive forces to add friction and viscosity
  - inertial force to add momentum
- Vibration
  - a signal indicating when the display should vibrate and at what frequency and amplitude

# Reference

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- An Interactive Introduction to Splines  
<http://www.ibiblio.org/e-notes/Splines/Intro.htm>
- Haptic Community Web Site <http://haptic.mech.northwestern.edu/>
- 3D audio <http://www.dcs.gla.ac.uk/research/gaag/dell/report.htm>
- VR audio [http://vrlab.epfl.ch/~thalmann/VR/VRcourse\\_Audio.pdf](http://vrlab.epfl.ch/~thalmann/VR/VRcourse_Audio.pdf)
- Scent <http://www.mis.atr.jp/past/sem/scent.html>